

The short-term association between environmental variables and mortality: Evidence from Europe

Jens Robben, Katrien Antonio, Torsten Kleinow

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UNIVERSITY
OF AMSTERDAM



RCLR

Research Centre
for Longevity Risk

Introduction

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 - temperature, e.g., Keatinge et al. [2000] and Basu and Samet [2002],
 - cold spells and heat waves, e.g., Braga et al. [2001] and Pattenden et al. [2003],
 - air pollution, e.g., Pascal et al. [2014] for PM10 and PM2.5 and Orellano et al. [2020] for ozone and nitrogen dioxide.

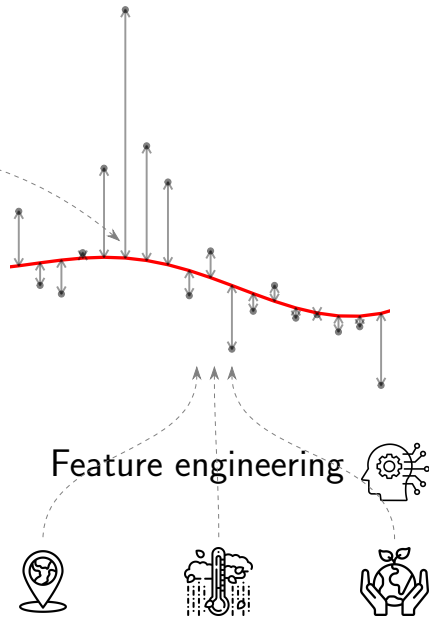
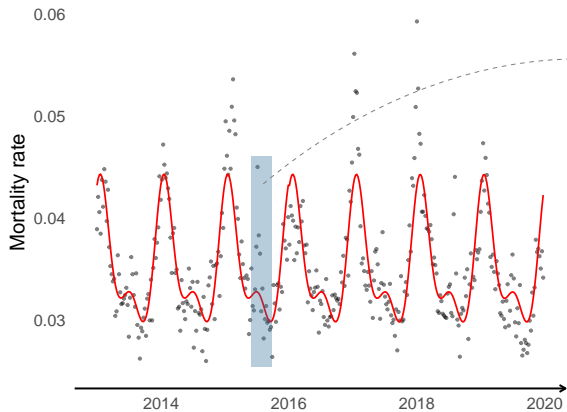
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Various methodologies have been proposed:

- Poisson regression models, e.g., Armstrong [2006] and Braga et al. [2002],
- Distributed Lag (Non-Linear) Models, e.g., Schwartz [2000] and Gasparrini et al. [2010],
- Extreme value analysis, e.g., Li and Tang [2022].

In this session, we will:

- try to explain weekly death counts across European regions
- with a baseline mortality model (e.g., alike EuroMoMo)
- combined with a (high-dimensional) set of weather and air pollution features
- constructed from publicly available data sources (e.g., Eurostat, CDS, CAMS, NASA's EarthData).

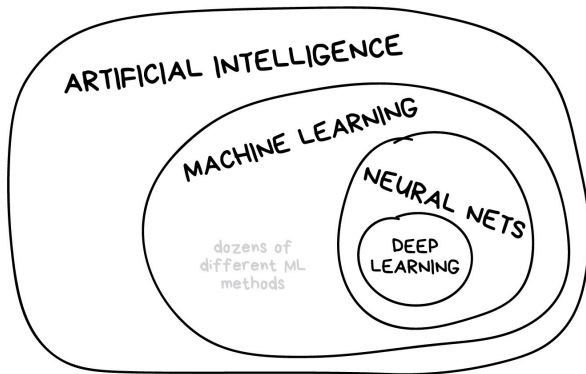


Machine learning and mortality modelling

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We will make use of machine learning methods to find associations between mortality and environmental data:

- death counts $D_{x,t,w}^{(r)}$ under Poisson assumption, in the presence of risk factors or covariates $\mathbf{z}_{x,t,w}^{(r)}$
- with techniques such as:
 - Random Forests (RFs)
 - Gradient Boosting Machines (GBM, XGBoost, LightGBM, ...)
 - Neural Networks (CANNs, ANNs, RNNs, ...).



Picture taken from [Machine learning for everyone. In simple words. With real-world examples. Yes, again.](#)

- Identify the **primary environmental factors** contributing to the estimation of mortality deviations from the baseline.
- Investigate the **marginal impact** of an environmental factor on deviations from the mortality baseline.
- Study how environmental factors **interact** when modelling mortality rates. Are there **harvesting** effects present?
- Demonstrate how to make **short-term mortality projections** with the model.

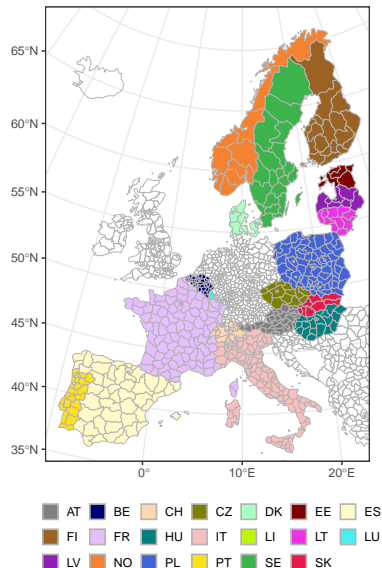
Data

Death counts

Eurostat: deaths by week, sex, 5-year age group and NUTS 3 region from 20 European countries throughout the years 2013-2019 (> 500 regions).

Focus on old age group 65+.

NUTS 3 regions

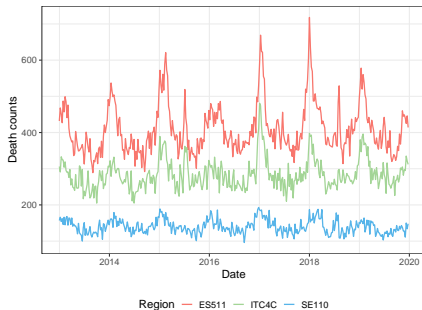


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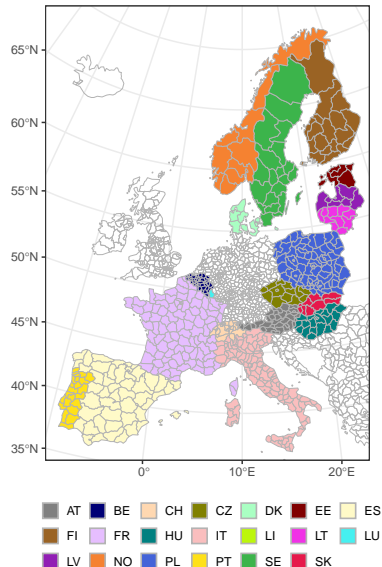
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Seasonal trend:



NUTS 3 regions



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Daily, high-resolution gridded dataset, defined on a grid with a spatial resolution of 0.10° (≈ 9 km).

Weather factors:

Tmax: daily maximum temperature.

Tmin: daily minimum temperature.

Hum: daily average relative humidity.

Rain: total daily precipitation.

Wind: daily average wind speed.

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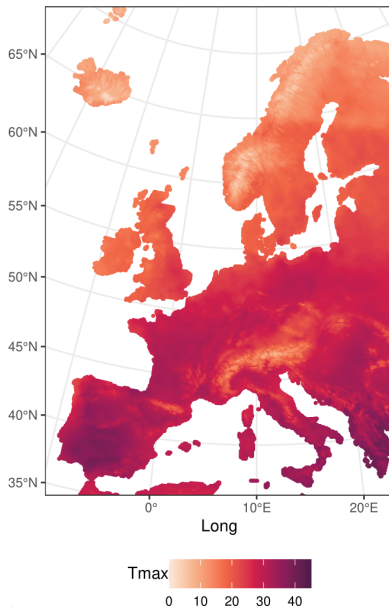
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Tmax: 2015-08-02



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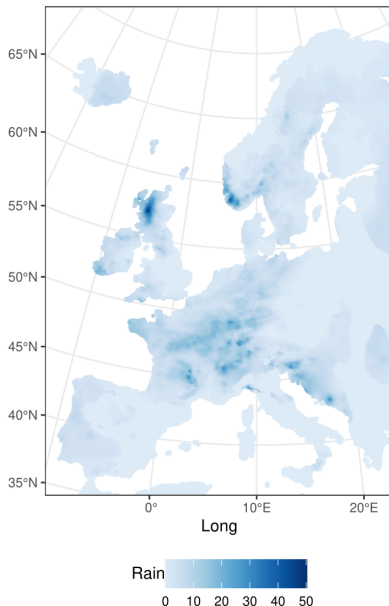
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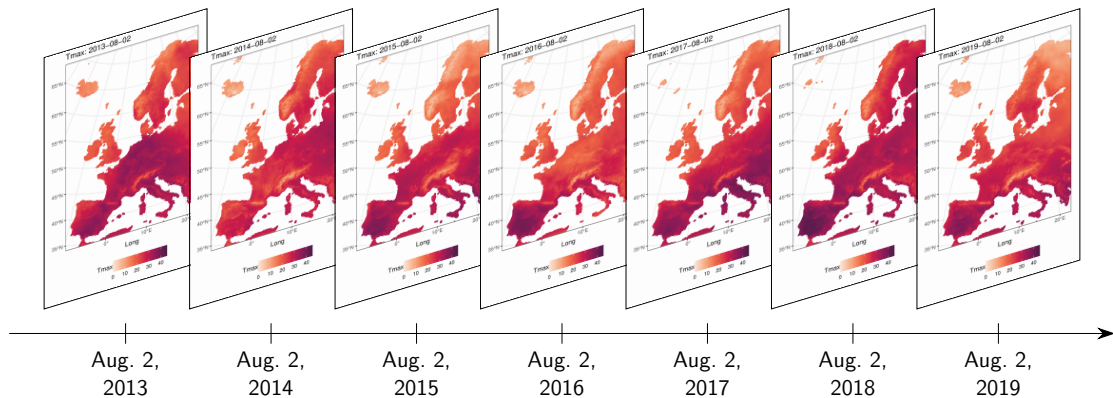
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Rain: 2014-02-13





Air pollution data

CAMS [European air quality reanalyses](#) dataset from the Copernicus Atmosphere Monitoring Service (land + sea).

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Air pollutants ($\mu g/m^3$):

O3: hourly [ozone](#) levels.

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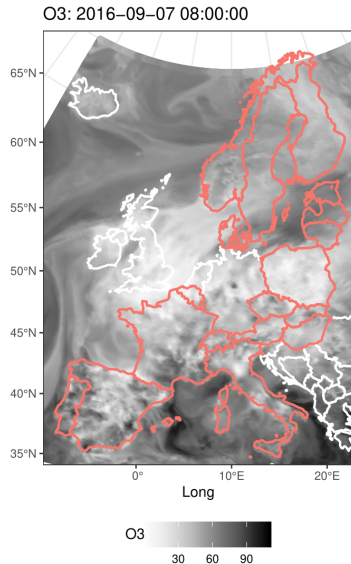
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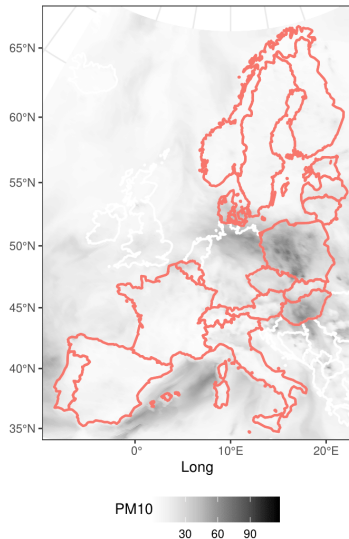
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PM10: 2019-02-01 10:00:00

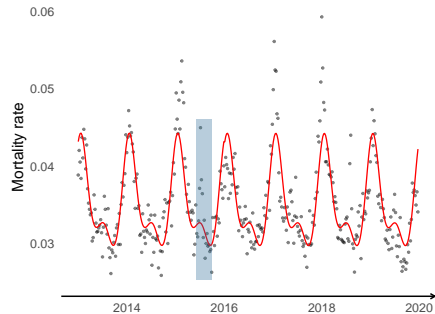


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Model specification

Weekly, region-specific baseline mortality model

A weekly, region-specific baseline mortality model to capture overall seasonal trends across all regions.

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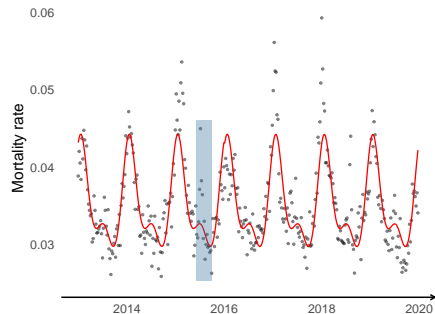
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Incorporate seasonality through Fourier terms
Serfling [1963]:

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$$\log \mu_{t,w}^{(r)} = \beta_0^{(r)} + \beta_1^{(r)} t + \beta_2^{(r)} \sin \left(\frac{2\pi w}{52} \right) + \beta_3^{(r)} \cos \left(\frac{2\pi w}{52} \right) +$$

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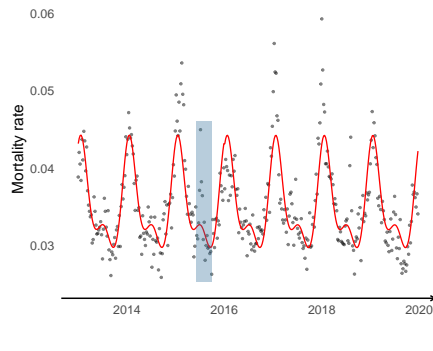
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Region-specific population exposures $E_{t,w}^{(r)}$ from Eurostat.



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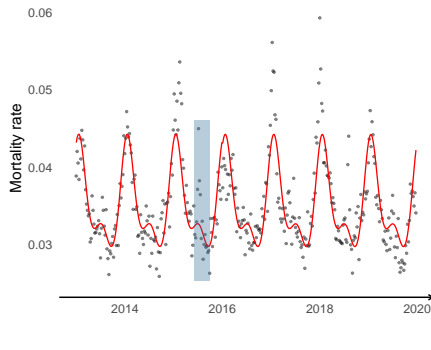
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Estimated baseline death counts: $\hat{b}_{t,w}^{(r)} := E_{t,w}^{(r)} \cdot \hat{\mu}_{t,w}^{(r)}$.

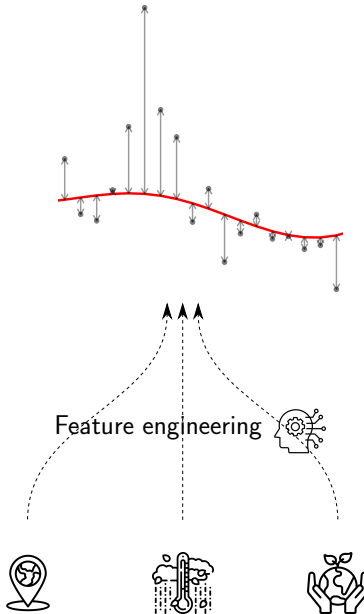


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Modelling deviations from the baseline model

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Explain observed deviations from the baseline deaths using region-specific environmental features.



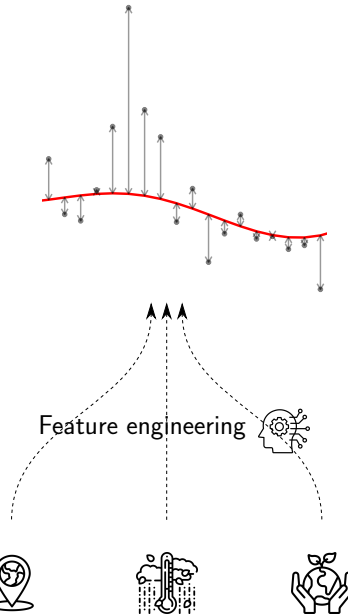
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Fix estimated baseline deaths and impose distributional assumption:

$$D_{t,w}^{(r)} \sim \text{Poisson} \left(\hat{b}_{t,w}^{(r)} \phi_{t,w}^{(r)} \right),$$

$$\phi_{t,w}^{(r)} = f \left(\text{long}^{(r)}, \text{lat}^{(r)}, \text{season}_{t,w}, \mathbf{e}_{t,w}^{(r)}, I^1 \left(\mathbf{e}_{t,w}^{(r)} \right), \dots, I^S \left(\mathbf{e}_{t,w}^{(r)} \right) \right).$$



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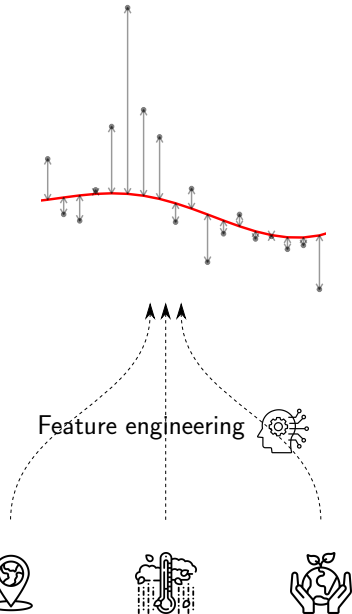
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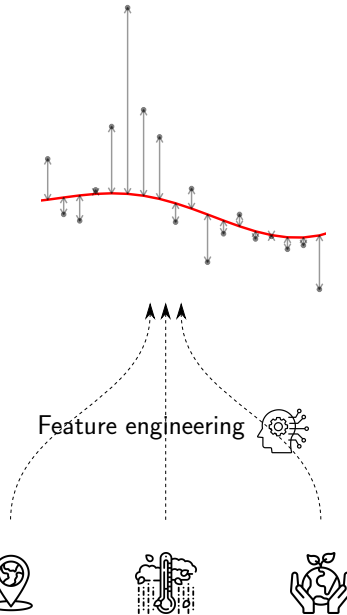
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Choice for machine learning model to identify non-linear relationships and potential interaction effects among environmental features.



Model calibration

Fit one **Poisson GLM** jointly on all regions, and add a **penalty term** to obtain **smooth variations** in the estimated parameters $\hat{\beta}_p^{(r)}$ across neighbouring regions:

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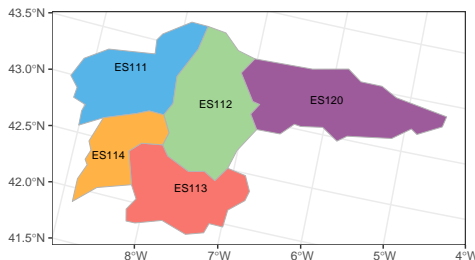
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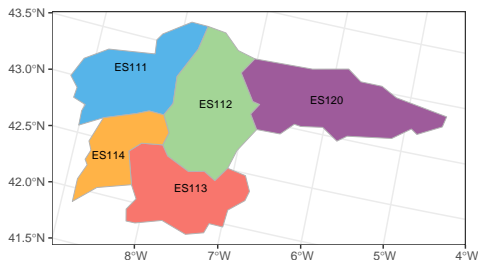
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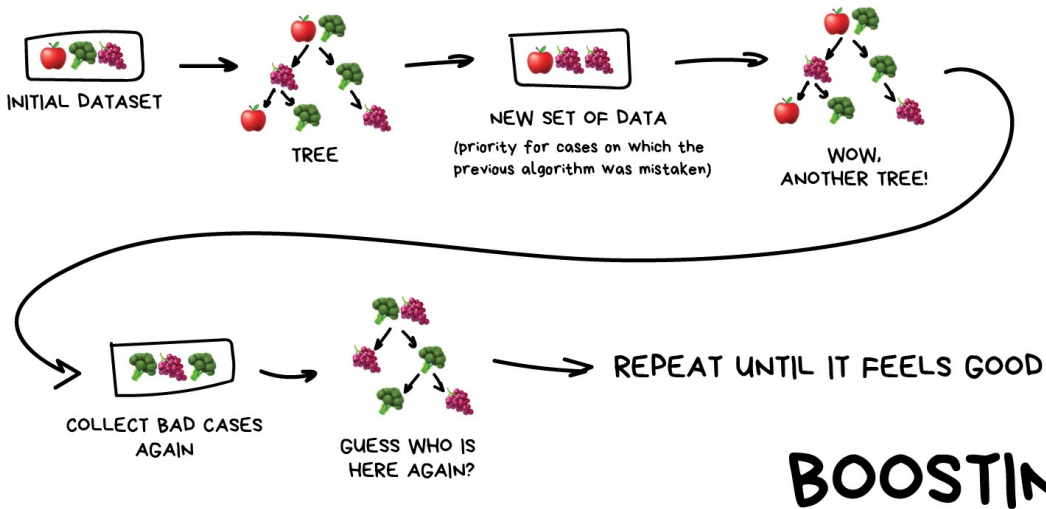


Penalty matrix \mathbf{S} :

$$\begin{matrix} & \begin{matrix} ES111 & ES112 & ES113 & ES114 & ES120 \end{matrix} \\ \begin{matrix} ES111 \\ ES112 \\ ES113 \\ ES114 \\ ES120 \end{matrix} & \begin{pmatrix} 2 & -1 & 0 & -1 & 0 \\ -1 & 4 & -1 & -1 & -1 \\ 0 & -1 & 2 & -1 & 0 \\ -1 & -1 & -1 & 3 & 0 \\ 0 & -1 & 0 & 0 & 1 \end{pmatrix} \end{matrix}.$$

Calibrating the mortality deviations via gradient boosting

14



Picture taken from [Machine learning for everyone. In simple words. With real-world examples. Yes, again.](#)

Parameter configurations

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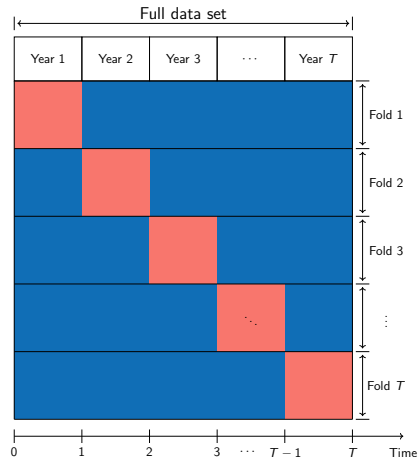
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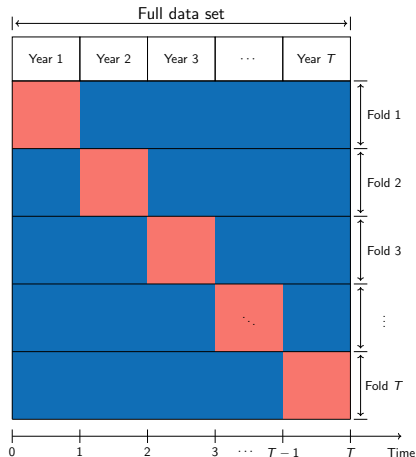
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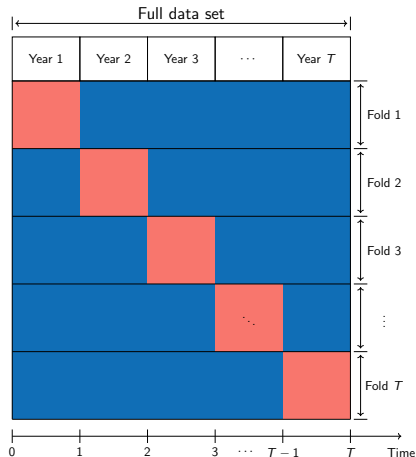
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Interpretation tools to gain insights: VIP, ALE.



Case study: feature engineering

Difference in spatial and temporal dimension:

- deaths data: weekly, NUTS 3 scale.
- environmental data: hourly or daily time scale, spatial grid.

Motivation

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Goal of feature engineering:

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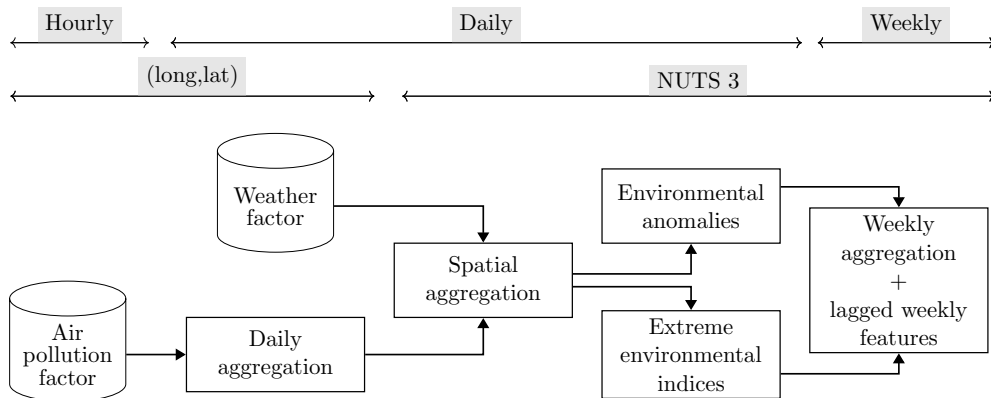
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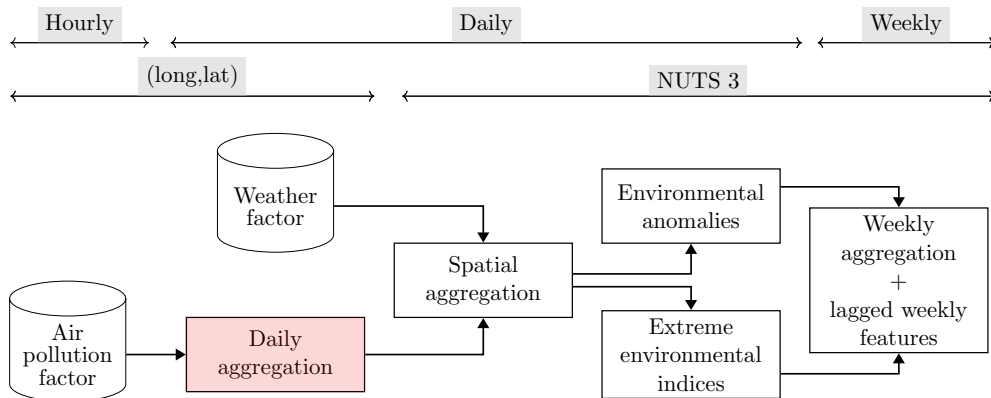
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- create features that measure deviations from baseline conditions from environmental data to explain excess or deficit mortality.





Consider an air pollution factor and denote its concentration at hour h of day d in week w of year t and located at longitude-latitude coordinates (long,lat) as $x_{t,w,d,h}^{(\text{long},\text{lat})}$.

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Compute the **daily minimum, average, and maximum** concentrations of the air pollutant, measured at the coordinates (long,lat) as:

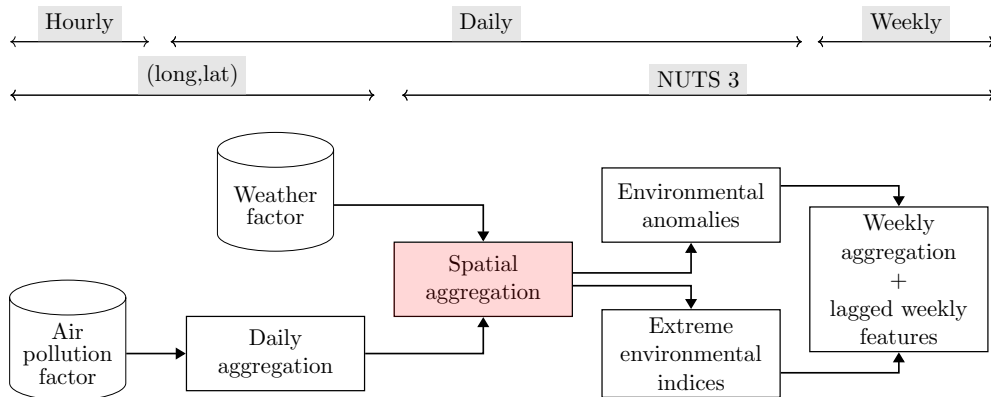
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Weather factors already available at the daily level (no need for daily aggregation).



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- $\omega_{(\text{long},\text{lat})}$: population weights using gridded population data from the Socioeconomic Data and Applications Center,

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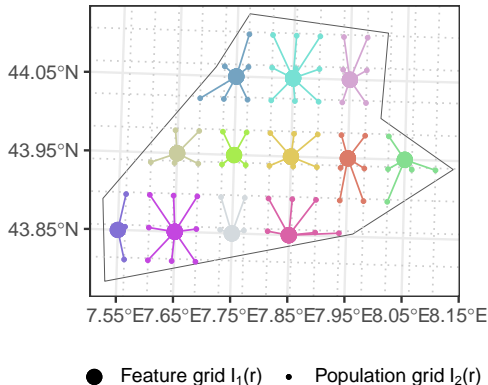
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where:

- $\omega_{(long,lat)}$: **population weights** using gridded population data from the Socioeconomic Data and Applications Center,

ITC31: Imperia



Spatial aggregation

$\tilde{x}_{t,w,d}^{(long,lat)}$: **daily level** of a specific environmental feature at **coordinates** (long, lat) for year t , week w , and day d .

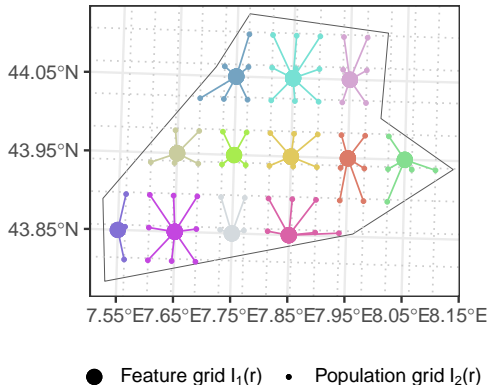
Construct **feature on NUTS 3 scale**:

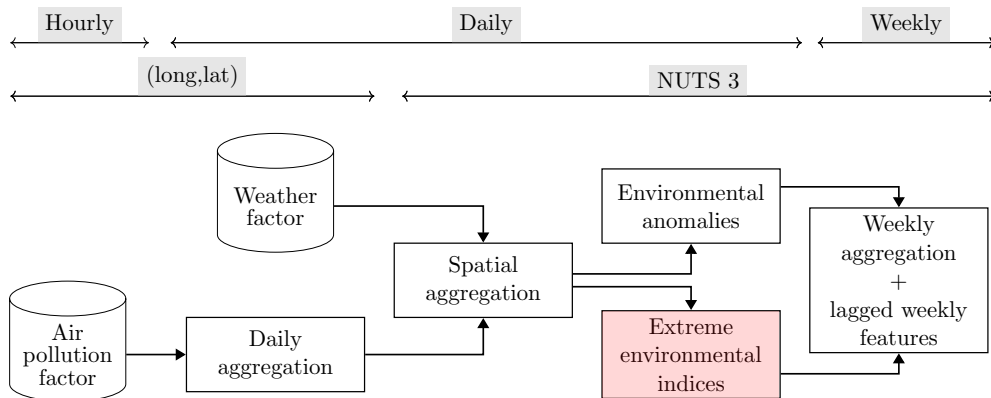
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- $\mathcal{I}_1(r)$: **feature grid** restricted to region r .

ITC31: Imperia





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Index values: 0-3, indicating the severity of hot days.

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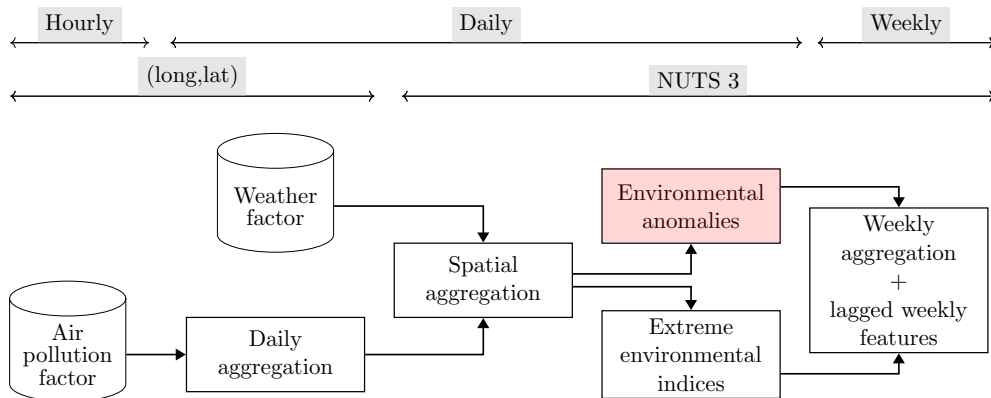
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Similar extreme indices are created for the remaining daily weather and air pollution factors.



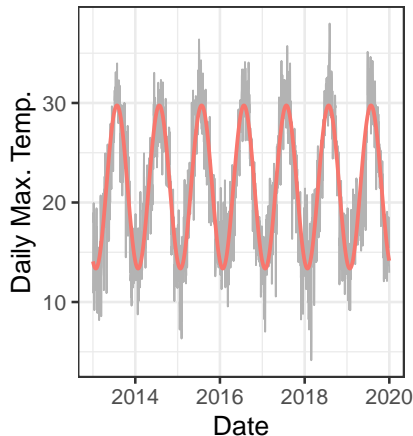
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Create features that **quantify deviations from typical, baseline conditions** for each day throughout the year.

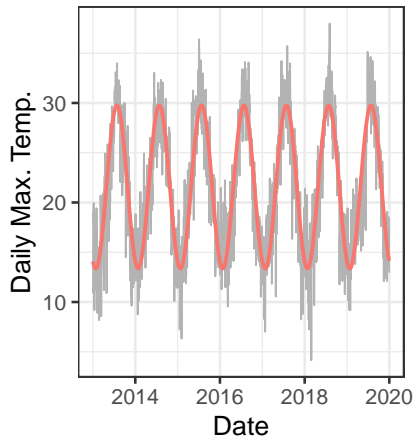
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In the paper, we work with excesses or deviations from the baseline (**anomalies**):

$$\tilde{x}_{t,w,d}^{(r)} - \hat{\tilde{x}}_{t,w,d}^{(r)}$$

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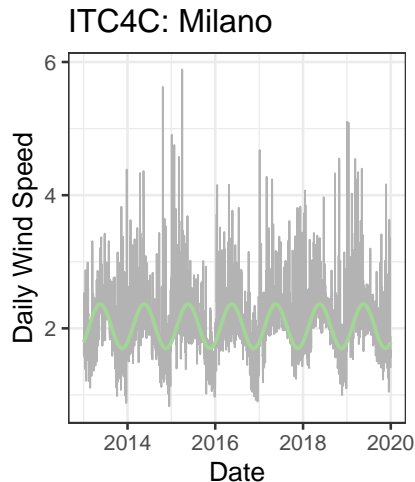
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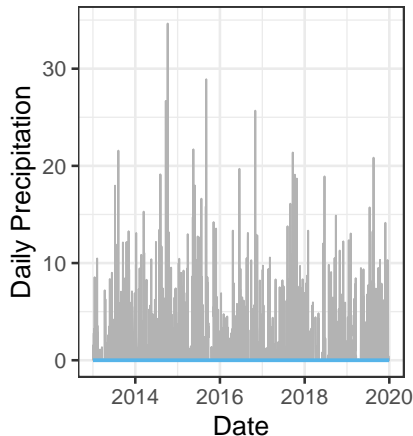
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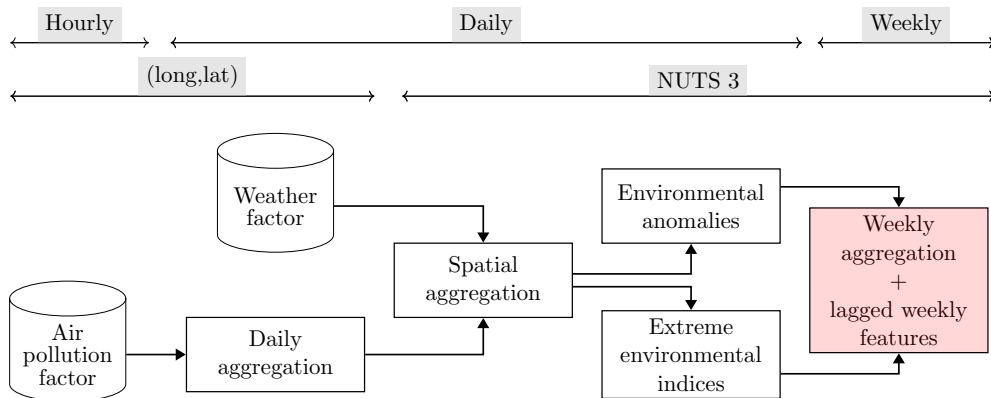
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Similar weekly aggregation techniques for remaining environmental anomalies and extreme environmental indices.

Weekly aggregation

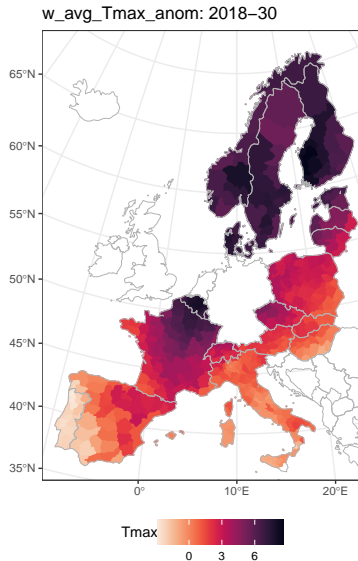
22

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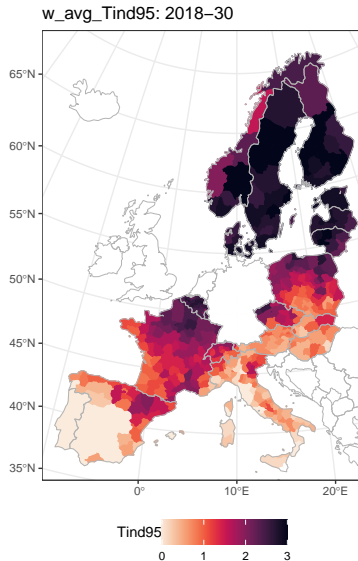


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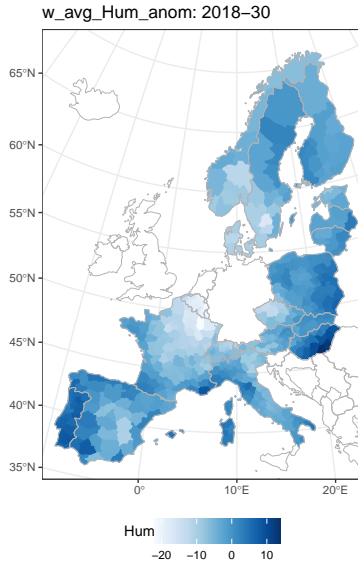


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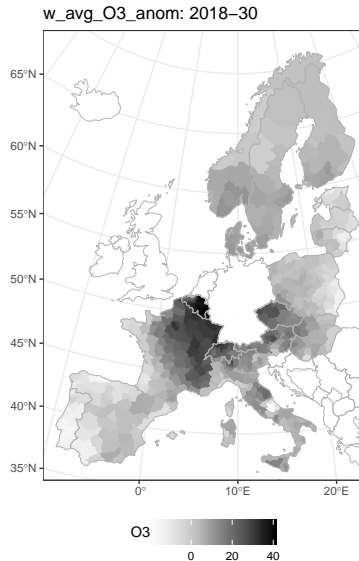


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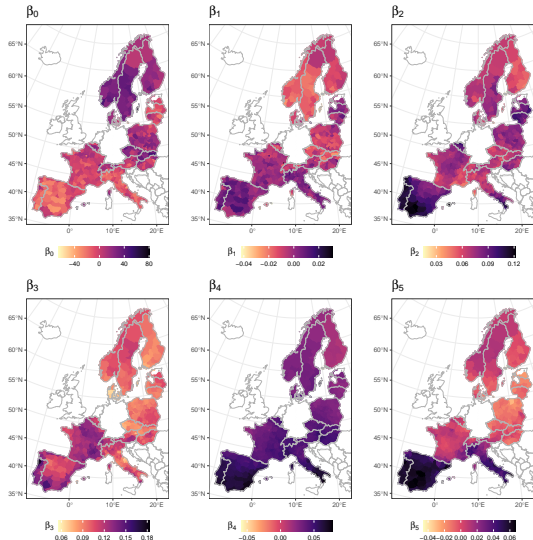
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Case study: calibration results

Baseline model



Machine learning model

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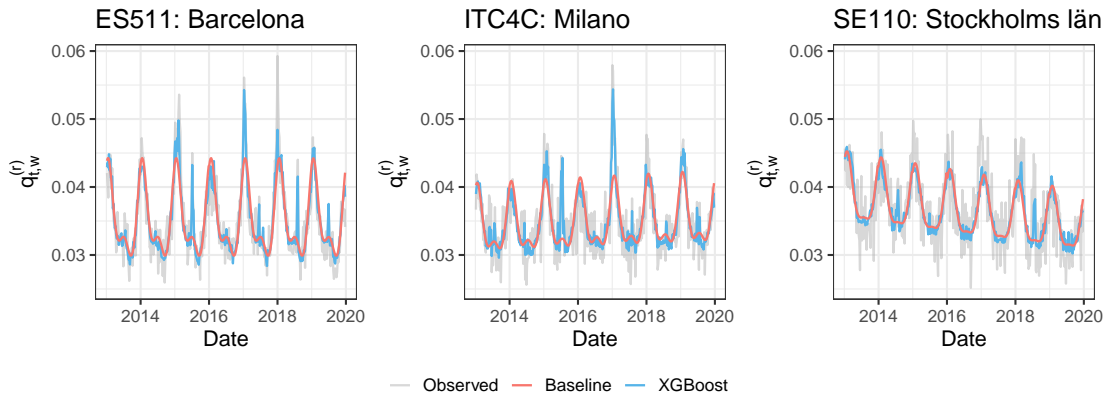
Input features: longitude-latitude coordinates, season, (one-week lagged) environmental anomalies and extreme indices.

Tuning by 7-fold cross validation over the years 2013-2019 using an extensive tuning grid.

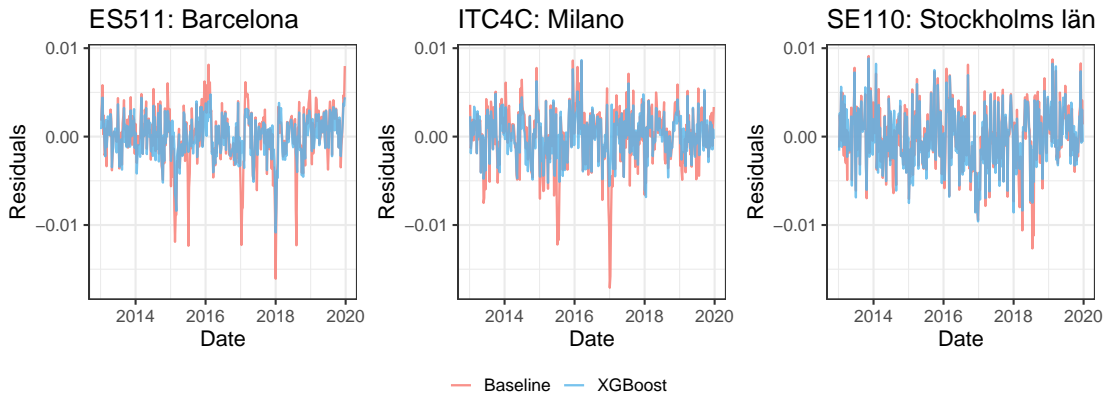
Tuning parameters: nrounds (490), eta (0.01), min_child_weight (1000), max_depth (7), subsample (0.75), colsample_bytree (0.50).

Insights in the machine-learning model

Observed and estimated mortality rates (baseline + XGBoost):



Residuals of the estimated weekly mortality rates (baseline + XGBoost):



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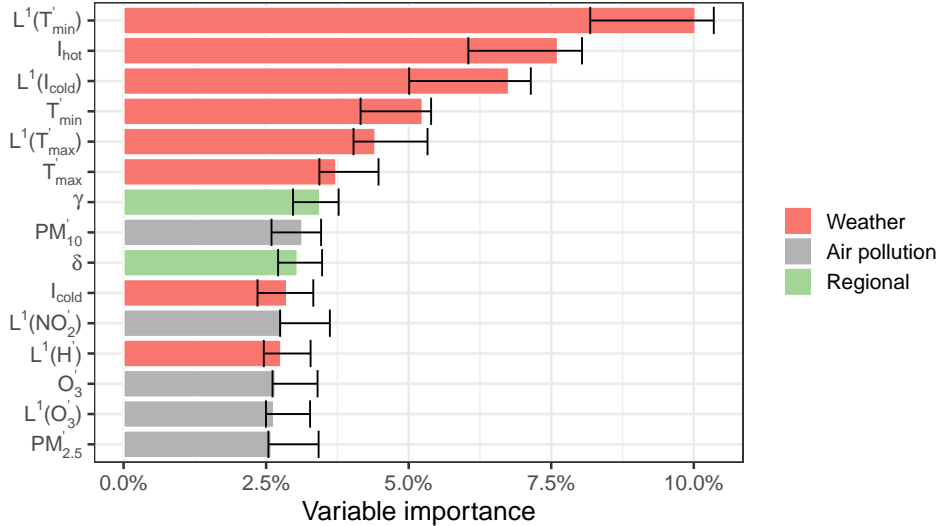
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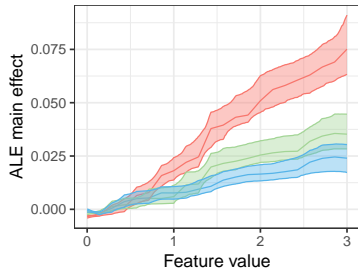
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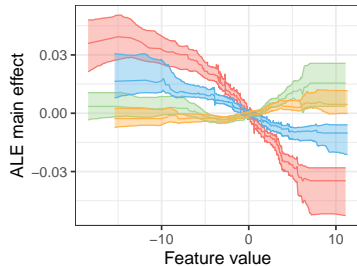
with $\Delta \mathcal{L}_n(X_l)$ the total reduction in the Poisson loss function, caused by splits associated to feature X_l in the tree built during iteration n of the XGBoost algorithm.

Features with a high importance appear **often** and **high** in the tree.

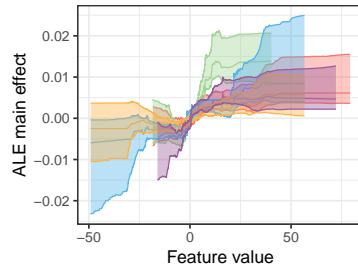




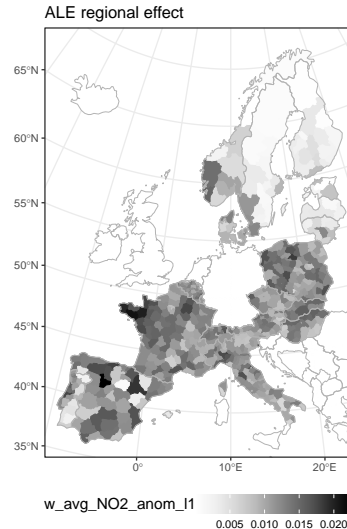
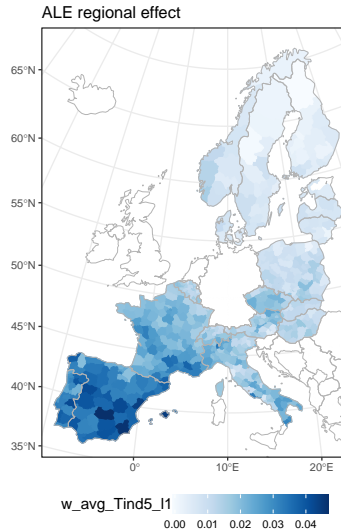
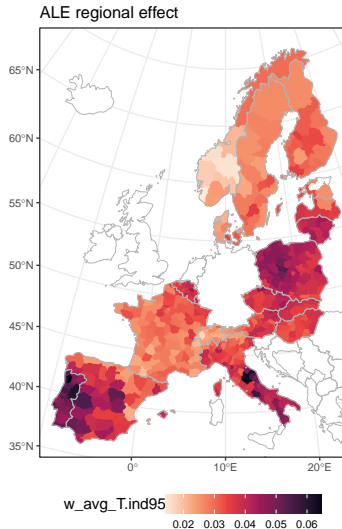
I_{hot} (7.62%) I_{cold} (2.86%)
 $L^1(I_{\text{cold}})$ (6.76%)

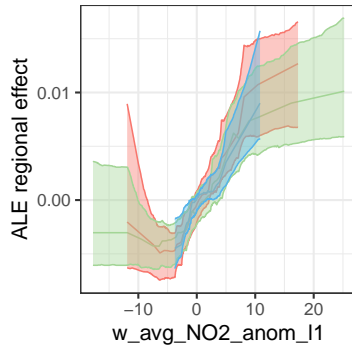
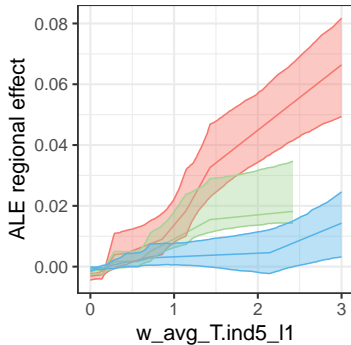
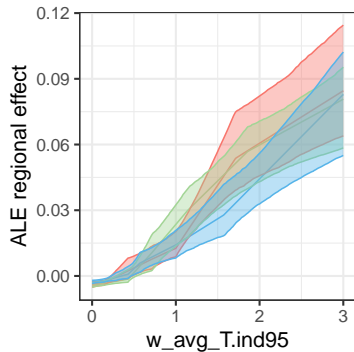


$L^1(T_{\text{min}})$ (10.03%) $L^1(T_{\text{max}})$ (4.41%)
 T_{min} (5.24%) T_{max} (3.73%)

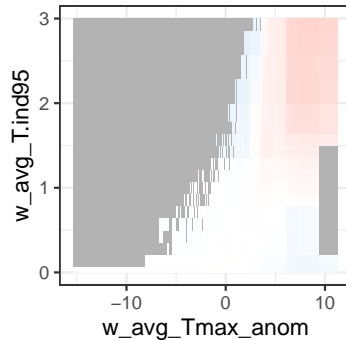
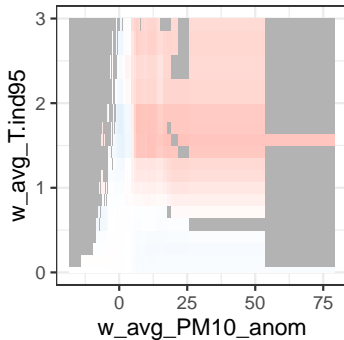
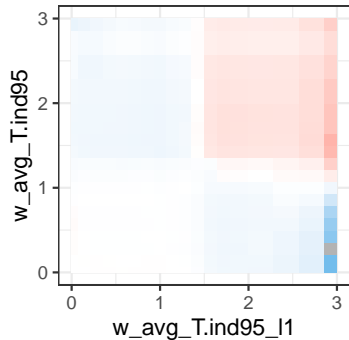


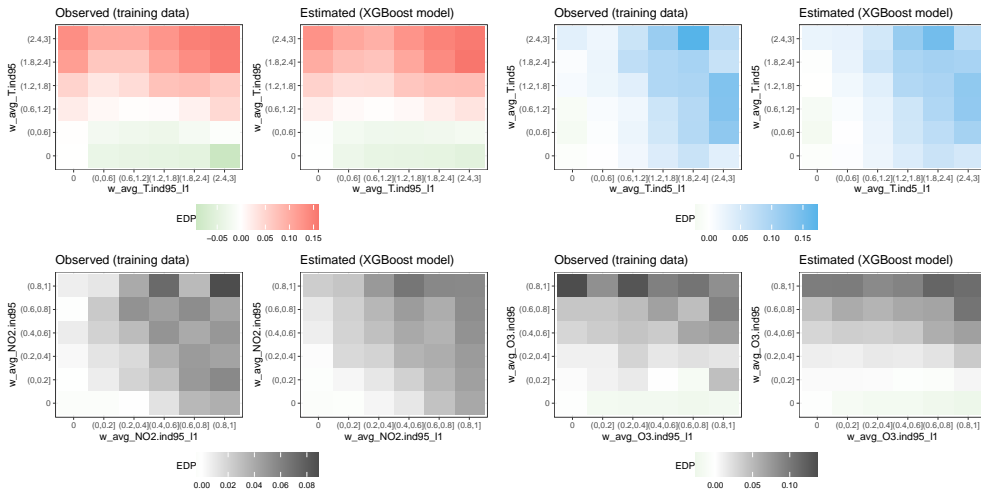
PM_{10} (3.13%) $L^1(O_3)$ (2.64%)
 $L^1(NO_2)$ (2.78%) $PM_{2.5}$ (2.59%)
 O_3 (2.66%)

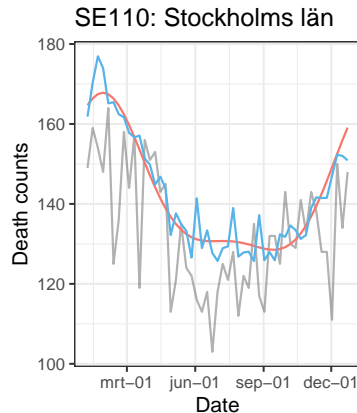
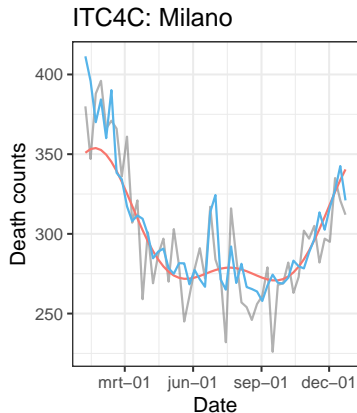
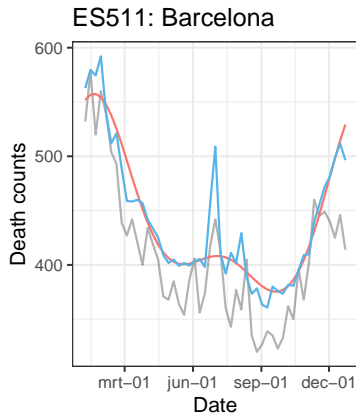




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— Observed — Baseline — XGBoost

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2. We highlight the advantage of incorporating the baseline number of death counts as an offset in the model. It makes our predictions more stable, robust, and interpretable, especially regarding statements about excess mortality.

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- Pablo Orellano, Julieta Reynoso, Nancy Quaranta, Ariel Bardach, and Agustin Ciapponi. Short-term exposure to particulate matter (pm10 and pm2. 5), nitrogen dioxide (no2), and ozone (o3) and all-cause and cause-specific mortality: Systematic review and meta-analysis. *Environment international*, 142:105876, 2020. doi: 10.1016/j.envint.2020.105876.
- Mathilde Pascal, Grégoire Falq, Véréne Wagner, Edouard Chatignoux, Magali Corso, Myriam Blanchard, Sabine Host, Laurence Pascal, and Sophie Larrieu. Short-term impacts of particulate matter (pm10, pm10–2.5, pm2. 5) on mortality in nine french cities. *Atmospheric Environment*, 95:175–184, 2014. doi: 10.1016/j.atmosenv.2014.06.030.

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